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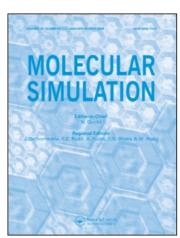
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# Molecular Simulation

Publication details, including instructions for authors and subscription information: <a href="http://www.informaworld.com/smpp/title~content=t713644482">http://www.informaworld.com/smpp/title~content=t713644482</a>

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To cite this Article Maus, Martin , Wagner, Karl G. , Kornherr, Andreas and Zifferer, Gerhard (2008) 'Molecular dynamics simulations for drug dosage form development: thermal and solubility characteristics for hot-melt extrusion', Molecular Simulation, 34: 10, 1197-1207

To link to this Article: DOI: 10.1080/08927020802411695 URL: http://dx.doi.org/10.1080/08927020802411695

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# Molecular dynamics simulations for drug dosage form development: thermal and solubility characteristics for hot-melt extrusion

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(Received 28 January 2008; final version received 12 August 2008)

Properties of pharmaceutical drug polymer mixtures like miscibility, stability and drug release are determined by the interactions of active pharmaceutical ingredients (APIs) and excipients (e.g. plasticisers) with functional polymers. Molecular dynamics (MD) simulations (Materials Studio<sup>®</sup>, COMPASS force field) are used to predict the principal behaviour of such drug products, especially miscibility and glass transition temperature ( $T_g$ ). Different mixtures containing APIs (theophylline or ibuprofen (IBU)) and water-soluble (triethyl citrate, (TEC)) or water-insoluble plasticiser (acetyl tributyl citrate (ATBC) or dibutyl sebacate (DBS)) dissolved/dispersed in a cationic polymethacrylate (EUDRAGIT<sup>®</sup> RS) were studied. Force field-based calculations of the cohesive energy densities of single constituents led to a qualitative approach according to Hanson describing the solid state of the mixture, while further calculations on the basis of the theory of free energy of mixing facilitated a semi-quantitative prediction. In the case of miscibility also calculation of  $T_g$  was possible via modelling specific volumes of amorphous cells at various temperatures. The simulated data correlated well with the experimental data obtained from differential scanning calorimetry (DSC) of drug products processed via hot-melt extrusion. Accordingly, the described method facilitates a good estimate of pharmaceutical polymer drug mixtures, thus decreasing product development time, as well as the consumption of active ingredients.

Keywords: drug dosage form; glass transition; plasticiser; polymer; solubility

#### 1. Introduction

In the last decade, the use of molecular dynamics (MD) simulations has become more and more familiar to pharmaceutical developers, e.g. by checking on polymorphisms [1,2] and calculating properties of host-guest complexes [3,4]. Furthermore, MD simulations can assist dosage form development by predicting valuable physicochemical properties like viscosity of solutions [5], diffusivity [6] and water adsorption [7]. However, the above-mentioned parameters are often limited to 'small' systems either related to the molecular weight of the drug compound or the excipient employed. The aim of our study is, therefore, to find in silico test models using MD methods for polymers, excipients, drugs and mixtures thereof exceeding standard MD applications in complexity, and hence facilitates preformulation even at a stage where the drug compound or polymer are in an in silico stage of development. Also, the risk of unexpected physical or chemical incompatibilities (e.g. immiscibility) during the formulation process, which is time consuming and expensive [8], might be decreased. Fortunately, molecular simulation offers the possibility to calculate many relevant

physical properties of the desired excipient and drug molecules, as well as of the polymer without the need of costly experiments.

In this respect, the *in silico* prediction of the thermodynamic mixing behaviour of different polymer—drug/excipient mixtures is of central interest. A common approach to cope with this problem is the calculation of the solubility parameters according to Hildebrand or Hansen [9–12], which is standard in the development of polymer mixtures [13]. The use of highly developed force fields as the basis of any MD simulation software enables the calculation of solubility parameters with an accuracy comparable with those measured experimentally by inverse gas chromatography [14], and an increasing number of other statistical quantitative property relationship between simulated and experimental values are established [15–18].

Focusing on polymer plasticiser blends, the glass transition temperature  $(T_{\rm g})$  is an important property in order to predict the formation of a solid solution. Homogeneous polymer plasticiser blends undergo a second-order-like phase transition at this temperature [19], passing from the

rubbery to glassy state with  $T_{\rm g}$  decreasing with increasing plasticiser concentrations [20,21]. Throughout the literature, several approaches to determine the glass transition temperature of polymers via computer simulations are reported based on the change in various physical properties at  $T_{\rm g}$ . One common approach is to determine the kink in a graph of the specific volume v versus temperature T [14,19,22–27], originating from the change in the thermal expansion coefficient. Other approaches also use the increase in potential energy [23–26] at  $T_{\rm g}$  or the temperature dependence of the mean square displacement of polymer chains below and above  $T_{\rm g}$  [26,28]. Normally, all these methods lead to a good prediction of  $T_{\rm g}$  values for *pure* polymers.

Simulations of pharmaceutical relevant *mixtures* of polymer/excipient/drug blends, however, are scarce. Momany and Willett [25] investigated the dependence of  $T_{\rm g}$  of maltodecaose on its hydration (water is known to act as a plasticiser for carbohydrates) and Yoshioka et al. [29] probed  $T_{\rm g}$  values of freeze-dried dextran cakes. Quite recently, we studied the  $T_{\rm g}$  dependence of an ammonio methacrylate copolymer (EUDRAGIT RS) as a function of its triethyl citrate (TEC) content [27], which was in good agreement when compared with experimental data.

In this follow-up study, we want to examine the miscibility and the impact on the drug dosage form in respect of  $T_{\rm g}$  from systems including EUDRAGIT RS (a cationic ammonio methacrylate copolymer, type B), three common plasticisers (TEC, acetyl tributyl citrate (ATBC) and dibutyl sebacate (DBS)) and two active ingredients: ibuprofen (IBU) (likely plasticising impact on EUDRAGIT RS [30]) and theophylline (unlikely plasticising influence on EUDRAGIT RS [31,32–34]).

The aim is to assist the developer in the two pivotal development questions of a hot-melt extruded dosage form.

- (1) What is the best polymer plasticiser mixture to obtain the lowest possible processing temperature for the extrusion process? A problem that is, of course, closely linked to a low value for  $T_{\rm g}$ .
- (2) What is the extent of the drug compound's solubility in the respective polymer plasticiser blend? The solubility should be rather high for the purpose of forming a solid solution to improve active pharmaceutical ingredient (API) solubility. And in contrast should be very low in case drug dispersion is intended to be formed to extend the API release from the polymer matrix.

In order to compare the simulated values with the hot-melt extrusion process, the feasible blends are produced through hot-melt extrusion, performed on a laboratory-scale ram extruder. Employing EUDRAGIT RS as a thermal polymer, which is known to form multiple-unit controlled-release matrix particles [20,34–36], the

purpose in respect of question 2 was to distinguish a system of low solubility for the drug compound.

#### 2. Materials and methods

All different substances used in this study are visualised in Figure 1 (all chemical structures are conformational, not optimised due to a better visibility).

#### 2.1 Materials

TEC was purchased from Merck KGaA (Darmstadt, Germany). The other substances were kindly donated by various manufactures: EUDRAGIT RS 100 by Röhm GmbH (Darmstadt, Germany), ATBC by Jungbunzlauer Ladenburg GmbH (Ladenburg, Germany), DBS by Morflex Inc. (Greensboro, NC, USA), IBU by Knoll Pharmaceuticals (Nottingham, UK) and theophylline anhydrous powder by BASF AG (Ludwigshafen, Germany).

#### 2.2 Numerical methods

# 2.2.1 Calculation of solubility parameters

In order to calculate the solubility of both plasticiser and drug molecules within a given polymer matrix, it is necessary to compute the so-called cohesive energy  $E_{\rm coh}$ . This energy is a measure of the intermolecular forces (both electrostatic and dispersive) acting between the molecules of a specific substance. Accordingly,  $E_{\rm coh}$  corresponds to the experimental value of the internal heat of vaporisation  $\Delta H_{\rm vap}$  (with R being the real gas constant) [10]

$$E_{\rm coh} = \Delta H_{\rm van} - RT. \tag{1}$$

In a computer simulation, the energy (and force) between different molecules is directly accessible from the force field. Therefore, it is possible to compute  $E_{\rm coh}$  directly and to transform it into the Hildebrand solubility parameter  $\delta$  [10] according to

$$\delta = \sqrt{\frac{E_{\rm coh}}{V}},\tag{2}$$

where V is the volume of the phase from which  $E_{\rm coh}$  is calculated.

For this numerical procedure, cubic simulation boxes (with periodic boundary conditions in all directions) containing either four polymer chains consisting of 62 monomer units each or 60 plasticiser/drug molecules are constructed. Dependent on the type of plasticiser, the cubic box size has a side length of *ca.* 4 nm (Figure 2). For each type of molecule, 10 independently generated simulation boxes are minimised with respect to the total energy. Out of those, the lowest energy system is further relaxed for

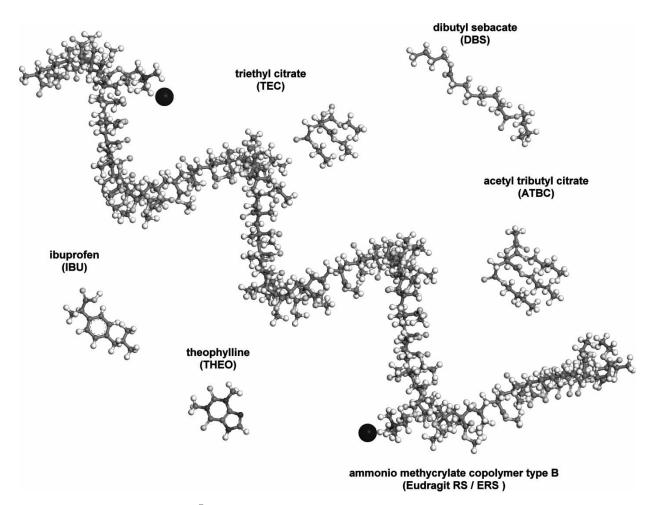


Figure 1. Visualisation of EUDRAGIT® RS polymer chain consisting of 64 monomers and all other molecules (both plasticisers and drugs) used in this study. The chlorine anion is depicted larger for better visibility; the different grades of grey in this and the following figures correspond to different atom types with white reserved for hydrogen, light grey for oxygen, grey for carbon and black for nitrogen or chlorine. All the graphical displays of molecules were generated with the Materials Visualizer (from Accelrys Inc.).

2 ns under *NPT* conditions at ambient conditions, i.e. at constant pressure  $(10^5 \, \text{Pa})$  and constant temperature (298 K) to obtain a well-relaxed start structure with the correct density using the Anderson thermostat and barostat [37], with a time step of 1 fs. Afterwards, a 200 ps run at constant volume and constant temperature (i.e., NVT conditions) is carried out  $-100 \, \text{ps}$  for equilibration and  $100 \, \text{ps}$  for data sampling. Thus, the cohesive energy is averaged over this latter period and the corresponding cohesive energy density  $E_{\text{coh}}/V$  is calculated by dividing it through the volume of the simulation cell.

During minimisation as well as during the MD runs, energy summation is performed in direct space making use of a group-based cut-off for non-bond interactions. Strictly speaking, a cut-off distance of 1.25 nm with a spline switching function is applied for the Coulomb and van der Waals interactions (the latter being expressed by a 6–9 Lennard-Jones potential) using charge groups to prevent dipoles from being artificially split when one of the atoms is inside and another outside a (atom-based) cut-off.

For the whole simulation procedure, the software package MS Modeling 3.0 (from Accelrys Inc., San Diego, CA, USA) was applied using the Amorphous Cell tool for construction of the amorphous phase and Discover as the MD code. Atomic charges and interactions between atoms and molecules were accounted for by the use of the COMPASS force field [38–41], which is highly optimised for the simulation of condensed phases.

# 2.2.2 Determination of the specific volume as a function of temperature

The numerical procedure is very similar to the method briefly described in Section 2.2.1 (see also [27]). However, now several independent starting structures (generally three to five, to average the obtained final specific volumes to decrease scatter) of the corresponding system are chosen and relaxed for 2 ns under NPT conditions at a temperature of approximately 100 K higher than the supposed glass transition temperature. Afterwards, a

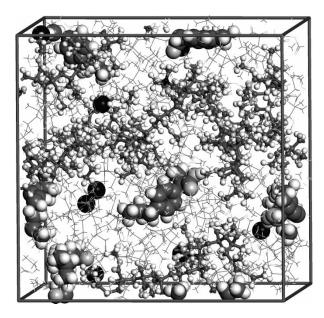


Figure 2. Simulation box  $(3.7 \times 3.7 \times 3.7 \text{ m})$  with periodic boundaries showing four EUDRAGIT RS polymer chains and six IBU molecules after a relaxation time of 2 ns at 430 K. One polymer chain and all IBU molecules are visualised in ball-and-stick style to demonstrate the size of the box, as well as the distribution of the drug molecules.

'cooling process' is initiated by lowering the temperature stepwise by  $10\,\mathrm{K}$  until a temperature  $\approx 100\,\mathrm{K}$  lower than  $T_\mathrm{g}$  is reached. At each temperature,  $200\,\mathrm{ps}$  NPT ensemble dynamics is carried out  $-150\,\mathrm{ps}$  for equilibration and  $50\,\mathrm{ps}$  for data sampling (i.e. averaging the specific volume v over this period) using the final configuration of this run as the starting structure for dynamics at the next ( $10\,\mathrm{K}$  lower) temperature.

## 2.3 Experimental methods

## 2.3.1 Hot-melt extrusion

According to the aim of the study, the mixtures of the polymer and its plasticising agents were produced by hotmelt extrusion at 140°C. The ram extruder, assembled by an in-house precision mechanic shop, consists of a massive brass cylinder with a 1200 W heat source connected to a self-adapting power controller KS40-1 (PMA Prozess-und Maschinen-Automation GmbH, Kassel, Germany) equipped with a PT100 sensor. The barrel diameter is 10.0 mm and the length 280 mm. By connecting a material testing machine DO-FB0.5TS (Zwick GmbH & Co, Ulm, Germany) to the plunger, it was possible to control and measure the force and velocity used for the extrusion of the hot melts through the orifice. The material testing machine was controlled by the utilisation of programmable logic arrays included in the software testXpert ver. 2.02 (Zwick GmbH & Co, Ulm, Germany).

About 10 g of the physical mixture, containing the polymer and the respective plasticising substance at quantities from 0 to 25.5% (w/w), were prepared. These mixtures were manually poured into the ram extruder and equilibrated for 10 min at 140°C. The stability of the polymer under the chosen conditions has previously been analysed by thermogravimetric analysis (TGA) measurements [35,42]. All mixtures were extruded three times at a plunger velocity of 15 mm/min through a 2.0 mm orifice.

# 2.3.2 Differential scanning calorimetry (DSC) measurements

DSC measurements were performed for the experimental determination of the glass transition temperature  $T_{\rm g}$ . The mean value of the onset and endset temperatures of the transition was calculated, according to DIN 53 765 A20. A Mettler TA 8000 calorimeter with a TAS 811 system and a DSC 820 measuring cell (Mettler-Toledo GmbH, Giessen, Germany) was used. Samples containing 20 mg polymer, including the respective plasticising substance, were accurately weighted and sealed in perforated 40  $\mu$ l Al pans and further analysed under a dry nitrogen purge at a flow rate of 50 ml/min.

### 3. Results and discussion

This section is divided into three parts:

- First, we will discuss the determination of solubility parameters in order to predict and explain polymer—plasticiser/drug miscibility. It is very important from both a theoretical and experimental point of view to ensure that two components are able to build a stable homogeneous mixture.
- Second, we will apply this knowledge to decide which of the possible polymer-plasticiser/drug systems are suitable for the calculation of T<sub>g</sub>.
- In the third part, the calculated  $T_{\rm g}$  values will be compared with experimental values.

# 3.1 Numerical determination of solubility properties

A computational method in combination with a suitable force field provides an advantage, in contrast to the commonly used group number systems [9,43] for calculating the solubility parameters according to Hildebrand [10] and Hansen [11]. Recent comparisons of simulated solubility parameters with those measured using reverse gas chromatography and other experimental methods [44] proved the accurateness of the simulated values.

All plasticisers used in this study are commonly used for the application of polymer coatings as well as for matrix systems [31–33,45–47]. TEC is the standard

plasticiser for EUDRAGIT RS with a maximum water solubility of 5%, underlining its hydrophilic character. ATBC was chosen due to its structural similarity compared with TEC, but with an increased lipophilic character. The third plasticiser, the double butylated decanedicarboxy acid (DBS), has a similar lipophilic character as ATBC, but the different molecular structure allows for an additional testing of our computational method.

IBU as a non-steroidal anti-inflammatory is reported to have plasticising properties in combination with EUDRAGIT RS [30], thus representing a model drug with severe interactions with the polymer matrix. Its aromatic molecular structure presents a further change in the geometry as well as in the hydrophilic-lipophilic character. By contrast, the anti-asthmatic methylxanthine theophylline has proved its inertness within formulations containing EUDRAGIT RS [31–34], and was therefore chosen as the second active ingredient in our study.

The physical states of the substances modelled differ at 298.15 K: DSC measurements (see also Section 3.3.2) show that polymer EUDRAGIT RS is amorphous without crystalline sections. By contrast, the plasticisers TEC, ATBC and DBS are fluids. Furthermore, the drugs IBU and theophylline are crystalline, with IBU melting within the hot-melt extrusion process while theophylline stays solid. These differences were taken into account for the calculation of the solubility parameters: using crystallographic data from the Cambridge Structural Database, it was possible to calculate the solubility parameters of both these crystalline drugs and the corresponding amorphous (i.e. molten) state.

#### 3.1.1 Hildebrand solubility parameters

The Hildebrand solubility parameters calculated within the MD simulation are presented in Table 1. As expected, crystalline drugs have the highest cohesive energy density with the Hildebrand parameter  $\delta$  (see Equation (2)), reading 31.64 (J/cm<sup>3</sup>)<sup>0.5</sup> for IBU and 51.43 (J/cm<sup>3</sup>)<sup>0.5</sup> for theophylline. By contrast, amorphous substances show

a reduced energy density due to the absence of the heat of crystallisation. With  $\delta$  reading 17.43 (J/cm<sup>3</sup>)<sup>0.5</sup>, the pure polymer has the lowest solubility parameter. The plasticisers and amorphous IBU are in the same range up to a maximum of 20.95 (J/cm<sup>3</sup>)<sup>0.5</sup> for IBU.

#### 3.1.2 Hansen solubility parameters

Hansen [11] divided the Hildebrand solubility parameter  $\delta$  into contributions from the non-polar van der Waals dispersion forces  $\delta_d$ , the polar (electrostatic) interactions  $\delta_p$  and the hydrogen bonding interactions  $\delta_h$ 

$$\delta^2 = \delta_d^2 + \delta_p^2 + \delta_h^2. \tag{3}$$

In most modern force fields like COMPASS, however, hydrogen bonding interactions are incorporated into the polar interactions; therefore, discrimination between  $\delta_p$  and  $\delta_h$  cannot be made. Accordingly, in our calculations, these parameters are combined to  $\delta_e$ 

$$\delta_{\rm e} = \sqrt{\delta_{\rm p}^2 + \delta_{\rm h}^2}. \tag{4}$$

The Hansen solubility parameters that were calculated according to Equation 4 are presented in Table 1. With  $\delta_{\rm d}$  values of ca. 17-19 (J/cm<sup>3</sup>)<sup>0.5</sup>, all plasticising molecules were within a narrow range; only the polymer seemed to have a reduced dispersive solubility parameter value reading 13.13 (J/cm<sup>3</sup>)<sup>0.5</sup>. A better discrimination was possible by comparison of the different values of the electrostatic interaction parameter  $\delta_{\rm e}$ : with a  $\delta_{\rm e}$  value of 11.32 (J/cm<sup>3</sup>)<sup>0.5</sup>, the pure polymer was in the same range, compared with amorphous IBU (11.89 (J/cm<sup>3</sup>)<sup>0.5</sup>) and the hydrophilic plasticiser TEC (8.62 (J/cm<sup>3</sup>)<sup>0.5</sup>), thus indicating an excellent miscibility. By contrast, both the values of DBS (3.29 (J/cm<sup>3</sup>)<sup>0.5</sup>) and ATBC (4.57 (J/cm<sup>3</sup>)<sup>0.5</sup>) showed an extended lipophilic character.

Extremely high values, however, can be observed when considering the crystalline state of the drugs theophylline and IBU with  $\delta_e$  readings of 45.85 (J/cm<sup>3</sup>)<sup>0.5</sup> and 26.53 (J/cm<sup>3</sup>)<sup>0.5</sup>, respectively. In addition, even the – only

Table 1. Overview of densities, molar volumes and solubility parameters calculated via MD simulations.

	$\rho$ (g/cm <sup>3</sup> )	$\nu_{\rm M}~({\rm cm}^3)$	$\delta \left( \text{J/cm}^3 \right)^{0.5}$	$\delta_{\rm e}~({\rm J/cm}^3)^{0.5}$	$\delta_{\rm d}~({\rm J/cm}^3)^{0.5}$
TEC	1.114	248.6	20.70	8.62	18.81
ATBC	1.039	387.5	17.96	4.57	17.37
DBS	0.910	345.4	17.63	3.29	17.32
IBU (amorphous)	0.977	211.2	20.95	11.89	17.25
IBU (crystalline)	1.092	188.9	31.64	26.53	17.23
THEO (amorphous)	1.350	133.5	29.48	16.99	24.10
THEO (crystalline)	1.493	120.7	51.43	45.85	23.29
ERS	1.028	6250.1	17.34	11.32	13.13

 $\rho$  (g/cm<sup>3</sup>), density;  $\nu_{\rm M}$  (cm<sup>3</sup>), molar volume;  $\delta$  (J/cm<sup>3</sup>)<sup>0.5</sup>, overall Hildebrand solubility parameter;  $\delta_{\rm e}$  (J/cm<sup>3</sup>)<sup>0.5</sup>, solubility parameter representing the electrostatic interactions, according to Equation 4;  $\delta_{\rm d}$  (J/cm<sup>3</sup>)<sup>0.5</sup>, solubility parameter representing the dispersive interactions, according to Hansen.

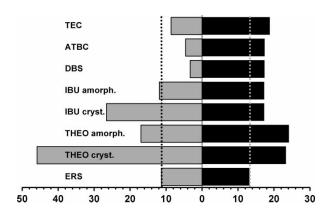


Figure 3. Visualisation of the dispersive  $\delta_d$  (right-hand side, black) and the electrostatic  $\delta_e$  (left-hand side, grey) solubility parameters, according to Hansen, with the upright dashed lines marking the values of the pure EUDRAGIT RS polymer.

hypothetical – amorphous state of theophylline showed a  $\delta_e$  value of 16.99 (J/cm<sup>3</sup>)<sup>0.5</sup> and a  $\delta_d$  parameter value of (24.10 (J/cm<sup>3</sup>)<sup>0.5</sup>. Therefore, no miscibility of this drug with the polymer could be expected. For ease of comparison of the different  $\delta_e$  and  $\delta_d$  values, a graphical representation is given in Figure 3.

# 3.1.3 Flory-Huggins interaction parameter

The qualitative considerations of the previous section regarding the solubility of plasticisers/drug/polymer blends can be transferred to a quantitative prediction of miscibility by calculation of the Flory–Huggins interaction parameter  $\chi$  [48]

$$\chi = \frac{V_{\text{ml}} \cdot (\delta_1 - \delta_2)^2}{R \cdot T},\tag{5}$$

 $V_{\rm m1}$ , molar volume of plasticising substance;  $\delta_1$ , solubility parameter of plasticiser;  $\delta_2$ , solubility parameter of polymer; R, 8.314472 J/(mol·K) (real gas constant); T, 298.15 K (absolute temperature).

An interaction parameter of zero describes an ideal solute–solvent system where the energetic interactions of two different molecules within a solution are equal to the interactions within the pure substance. The higher the value of  $\chi$  the more dissimilar are the two substances, and therefore will not easily dissolve each other.

The calculation of this interaction parameter of different substances and the polymer displayed the

differences as well as similarities of the studied blends (Table 2). For all classic plasticisers, the Flory–Huggins parameter  $\chi$  was equal to or less than 1.132 when mixed with the polymer. For the crystalline drugs IBU and theophylline,  $\chi$  would read 56.6 and 15.5, respectively, whereas the corresponding amorphous states show an extreme decrease in  $\chi$  reading 1.1 and 7.9.

#### 3.1.4 Gibbs free enthalpy change of mixing

The Gibbs energy of mixing  $\Delta G_{\rm m}$  [48] describes the overall thermodynamic benefit of generating a polymer–plasticiser mixture. Mixing of two substances only occurs in the case of negative values of  $\Delta G_{\rm m}$ . As a molecular solution of the plasticiser in the polymer matrix is an indispensable requirement for its plasticising properties, the possibility to calculate the value of  $\Delta G_{\rm m}$  prior to the specific experiment is extremely helpful in practice.

$$\Delta G_{\rm m} = k \cdot T \cdot \left( \frac{N}{V_{\rm m1}} \cdot v_1 \cdot \ln v_1 + \frac{N}{V_{\rm m2}} \cdot v_2 \cdot \ln v_2 + \chi \cdot \frac{N}{V_{\rm m1}} \cdot v_1 \cdot v_2 \right), \tag{6}$$

k,  $1.38 \cdot 10^{-23}$  J/K (Boltzmann constant); T, 298.15 K (absolute temperature); N,  $6.02 \cdot 10^{23}$  mol $^{-1}$  (Avogadro constant);  $V_{\rm m1}$ , molar volume of plasticising substance;  $V_{\rm m2}$ , molar volume of polymer chain;  $v_1$ , 0.1 (volume fraction of plasticiser);  $v_2$ , 0.9 (volume fraction of polymer).

In Table 2, the  $\Delta G_{\rm m}$  values calculated according to Equation (6) for different polymer–plasticiser systems with a typical value for the plasticiser volume fraction of 10% are presented. As expected from the solubility parameters, these values are positive for the crystalline drugs and even for the hypothetical amorphous state of theophylline. Therefore, further simulations (and experiments) considering the plasticising properties of theophylline made no sense.

### 3.2 Simulation of plasticising properties

The glass transition temperatures of all substances that show a possible molecular miscibility with the polymer matrix were simulated. As described in the numerical section, a previously reported MD method [27] was applied.

Table 2. Calculated Flory-Huggins parameter  $\chi$  and free enthalpy of mixing  $\Delta G_{\rm m}$  of 10% excipient with 90% polymer at 298 K.

	TEC	ATBC	DBS	IBU (amorphous)	IBU (crystalline)	THEO (amorphous)	THEO (crystalline)
$\frac{\chi}{\Delta G_{\rm m}  ({\rm J/cm}^3)}$	1.132	0.060	0.012	1.111	15.582	7.939	56.584
	-1.318	-1.476	-1.682	- 1.566	15.343	9.965	99.846

# 3.2.1 Different polymer/TEC solid-state solutions

The first check of our improved model (four instead of eight polymer chains, but with a doubled chain length) for the MD simulations was a recalculation of  $T_{\rm g}$  of the previously simulated [27] polymer–TEC systems. Again, a cooling of the new model of the pure polymer from 480 to 250 K in 10 K steps showed a clearly visible kink in the specific volume v versus temperature T diagram (Figure 4(a)), thus indicating a second-order-like phase transition from the rubbery to glassy state. The glass transition temperature (354 K) was indicated by the interception of two linear regression lines from the rubbery and glassy phase.

Analogous to the previous work [27], mixed systems containing four long polymer chains plus 6 or 12 TEC molecules per simulation box were constructed and the corresponding  $T_{\rm g}$  values were determined (Figure 4(b), (c)): 332 K for the 6 TEC system and 308 K for 12 TEC system. Accordingly, the improved new model for the MD simulation of the TEC containing EUDRAGIT RS systems showed a nearly perfect linear correlation of a decreasing value of  $T_{\rm g}$  at an increasing plasticiser concentration (Figure 5).

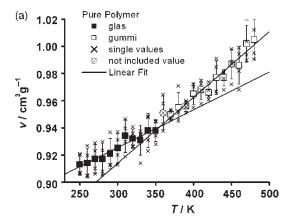
Although some deviation from experimental DSC data still occurred, the comparison with the previously reported [27] short-chain system (dotted line in Figure 5) clearly highlights the improvement of doubling the polymer chain length in the new model used in this work.

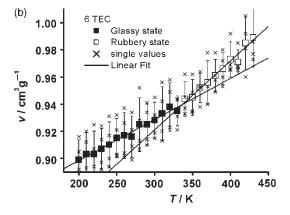
## 3.2.2 Further solid polymer-plasticiser solutions

Due to the good reproducibility of calculated and experimental  $T_{\rm g}$  values of the plasticiser TEC, the more lipophilic plasticisers ATBC and DBS as well as the model drug IBU were also tested. Amorphous cells containing four polymer chains and six molecules of either ATBC, DBS or IBU were constructed and the corresponding  $T_{\rm g}$  values were determined by analysing the kink in the v versus T diagrams (Figure 6).

All data points within the simulated temperature range of ATBC were included for the subsequent analysis. Due to the distinct kink in the v versus T graphs, it was easy to separate them into two parts (a rubbery and a glassy part) and fitting them to a straight line by linear regression (Figure 6(a)). By contrast, data points of both DBS and IBU showed a larger temperature interval where the glass transition seems to take place. This was indicated by larger deviations from the linear regression lines in the rubbery as well as in the glassy state. Accordingly, some values in this region without a clear defined physical state (rubbery or glassy) have been left out for analysis (Figure 6(b),(c)).

In Table 3, the calculated and the DSC measured glass transition temperatures of all simulated systems are presented. As expected, simulated  $T_{\rm g}$  values were always higher than the experimental values due to the high cooling rate in a computer experiment (i.e. in an *in silico* 





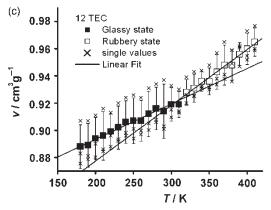


Figure 4. Plot of the computed specific volume v of (a) pure EUDRAGIT RS polymer, (b) EUDRAGIT RS polymer and 6 TEC as well as (c) 12 TEC molecules per simulation box versus temperature T of the system. The intersection point of the two lines resulting from a linear regression of the data points corresponding to the glassy ( $\blacksquare$ ) and rubbery ( $\square$ ) states determines the simulated  $T_g$  values (Table 3). All values are means of the specific volumes at the specified temperature of at least three independent systems; printed error bars represent the SD and circles represent values not used in the analysis.

experiment one could regard the system as being 'shock frozen'). However, the discrepancies were only 4-11%, thus indicating the reliability of the presented computational method.

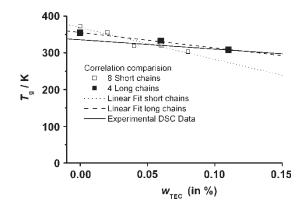


Figure 5. Comparison of the dependence of the glass transition temperature  $T_{\rm g}$  on the TEC weight proportion  $w_{\rm TEC}$  determined by the new MD model (filled symbols, dashed line), the MD model used in our previous communication (open symbols, dotted line) and experimental (solid line) DSC values. All lines result from a linear regression of the data points.

# 3.3 Experimental check of the plasticising properties

# 3.3.1 Production of solid solutions using a hot-melt ram extruder

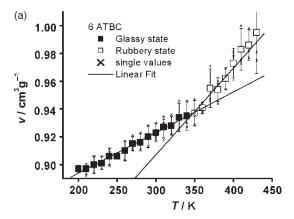
All physical mixtures were extruded at the conditions stated in the experimental section. By subsequently extruding the mixtures three times, enough shear was applied to achieve well-distributed solid solutions of the plasticisers within the polymer matrix. A comparison of the development of the force effect during the extrusion cycles showed a reduction in the force effect at each step. This trend clearly indicated that the homogeneity increased through the multiple ram extrusion. Furthermore, all three plasticisers, TEC, ATBC and DBS showed either extreme stickiness, or a too soft consistency of the extruded polymer strands at levels higher than 25.5%. Therefore, a plasticiser fraction *w* of 25.5% (m/m) indicated the endpoint in the application range.

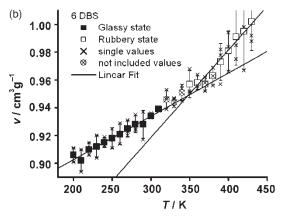
The crystalline drug IBU melts at  $76^{\circ}$ C, so the applied extrusion temperature allowed the incorporation of molten drug into the polymer matrix. Therefore, IBU could be homogeneously dissolved up to the values of w reading 20% (due to the high stickiness, no higher solid-state solutions could be produced).

By contrast, theophylline is melting at 270°C, so this drug remained crystalline during the entire hot-melt extrusion process and was only suspended in the polymer matrix. The compositions and glass transition temperatures of all samples produced by hot-melt extrusion are shown in Table 4.

#### 3.3.2 Thermal analysis of the extrudates

The subsequent DSC measurements of the produced polymer-TEC, polymer-ATBC and polymer-DBS





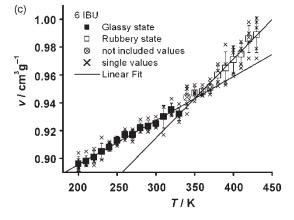


Figure 6. Plot of the computed specific volume v versus temperature T of three different polymer–plasticiser systems, each containing four polymer chains and (a) six ATBC, (b) six DBS, and (c) six IBU molecules per simulation box. Symbols and determination of  $T_{\rm g}$  are as in the legend of Figure 4 (values can be found in Table 3).

extrudates, up to a weight percentage of 19%, showed a clearly visible, strictly amorphous step when the heat flow was plotted against the reference temperature T. A representative DSC plot of the transition of the pure polymer as well as a polymer–TEC extrudate at 17% is shown in Figure 7.

•	C									
	ERS		TE	EC	IB	U	DI	BS	AT	ВС
n	DSC	MD								
0	336.7	354								
6			320.2	332	328.5	349	315.9	348	316.3	353
12			306.5	308						

Table 3. Overview of extrapolated experimental and calculated  $T_{\rm g}$  values in Kelvin of the different polymer/plasticiser systems with n symbolising the number of plasticiser molecules per simulation box.

As it was reported earlier for other polymer/plasticiser blends [27,30,34,42,45], the measured  $T_{\rm g}$  values of the extrudates exhibited a linear dependence on to the mass fraction w of plasticiser in the melt. Furthermore, all the plasticisers studied in our work showed a good experimental solubility in the acrylic copolymer EUDRAGIT RS, thus resulting in homogeneous solid solutions by the application of the ram extruder.

However, as one could already mention within the qualitative comparison of the Hansen parameters in Table 1 and Figure 3, there exists a limit of solubility of plasticisers like DBS in the polymer matrix (at weight percentage of 19%). This could be proved by the DSC measurements of matrices containing 21.5% of DBS; a representative plot is presented in Figure 8. In contrast to homogeneous polymer/plasticiser blends where an amorphous step in the heat flow versus temperature plot is visible, a dent – marking the melting point of the plasticiser DBS – occurs on the plot. Therefore, this mixture actually existed of two different, only mechanically mixed, phases: a polymer and a plasticiser phase.

IBU exhibited a similar behaviour like the three plasticisers: again, a linear correlation of the weight proportion of IBU and the  $T_{\rm g}$  of the matrix was found as it was also reported by Kidokoro et al. [34] that its ability to plasticise EUDRAGIT RS was slightly lower, compared with the plasticisers.

Table 4. Composition and experimental  $T_{\rm g}$  values of all samples produced by hot-melt extrusion.

Polymer (%)	TEC (%)	ATBC (%)	DBS (%)	IBU (%)	$T_{ m g}  m (K)$	SD
100					336.7	0.6
89	11				305.3	0.9
85	15				300.9	1.2
78	22				280.4	1.1
90		10			310.0	0.6
86		14			303.9	1.4
79		21			289.7	0.9
91			9		304.6	0.5
85			15		296.1	0.5
81			19		285.0	1.7
90				10	318.5	0.3
80				20	300.5	0.9

By contrast, theophylline did neither influence the glass transition temperature of the pure polymer nor of the investigated polymer/plasticiser mixtures, which is in good agreement with previous works [30,34].

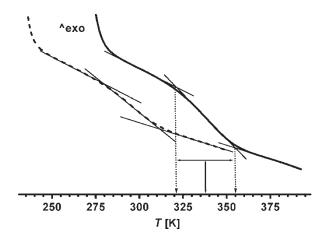


Figure 7. Plot of the heat flow against temperature T in a DSC experiment of a pure polymer (solid line) as well as a polymer—TEC mixture (dashed line) with w = 17%. Both show a distinct step in the heat flow, marked by the onset/endset point with the midpoint between these two yielding the experimental value of the glass transition temperature  $T_{\rm g}$ .

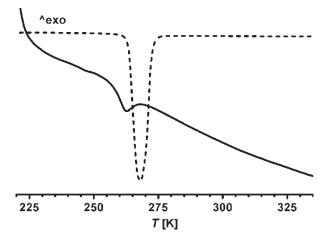


Figure 8. Plot of the heat flow against temperature T in a DSC experiment of a polymer–DBS mixture (solid line) with w = 21.5%, as well as of pure DBS (dashed line). The melting peak of DBS is also visible in the polymer–DBS curve, thus indicating the existence of two different phases.

#### 4. Conclusion

Our study shows that solubility properties of different polymer–plasticiser/drug blends can be calculated by the application of MD simulations using a proper force field. However, Hildebrand's parameter  $\delta$  leads to an incomplete picture of the solubility property of a given system, e.g. polymer–DBS; although this lipophilic plasticiser exhibited nearly the same solubility parameter  $\delta$  as the polymer (indicating a nearly ideal mixture), it showed an experimental solubility limit at higher plasticiser fractions. By contrast, solubility parameters, according to Hansen, deliver a more detailed picture by splitting  $\delta$  in a dispersive  $\delta_{\rm d}$  and an electrostatic  $\delta_{\rm e}$  component: now, due to the large difference of  $\delta_{\rm e}$  between the polymer and the plasticiser, a solubility limit could be explained at least qualitatively.

However, a final decision as to whether a substance has the theoretical potential to build a stable blend with the polymer or not can only be made by calculating the Gibbs energy. As shown in Table 2, only TEC, ATBC, DBS and amorphous IBU showed a theoretical miscibility with the polymer. This was also proved by experiments studying hot-melt extrudates.

Based on these solubility calculations, only miscible polymer-plasticiser/drug systems were further investigated with respect to their plasticising properties. The correlation of the simulated  $T_g$  values with the experimental ones reflects the different solubility behaviours of the plasticisers studied: less miscible plasticisers like DBS and ATBC show a higher deviation from the experimental  $T_g$  values, while the good soluble plasticiser TEC, as well as the amorphous drug IBU, exhibits markedly less differences. Accordingly, it seems as if the modelling of the glass transition of polymer-like plasticisers results in a better agreement with experimental values compared with the less miscible substances. With the maximum discrepancies between simulated and experimental values being not more than 11% in the worst case, the validity of our improved computer model is demonstrated. Thus, it is possible to make predictions of the glass transition temperature of these systems with high precision.

As a concluding remark, it can be stated that our method gives pharmacists a valuable recipe of how to treat unknown polymer–plasticiser/drug systems with respect to their mixing and plasticising properties. The benefit of the presented method is a direct reduction of time expenditure and costs, in relation to the present trial and error principle in dosage form development.

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